

Section 9.3 Special Properties of Binomial Multiplication

Goal • Use special product patterns to multiply polynomials.

Square of a Binomial Pattern

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

Example 1: Find the product

a. $(x + 3)^2$

$$(x+3)(x+3)$$

FOIL

$$x^2 + 6x + 9$$

b. $(x - 4)^2$

$$\begin{array}{cc} | & | \\ a & b \end{array}$$

$$a^2 - 2ab + b^2$$

$$x^2 - 2(x)(4) + 4^2$$

$$x^2 - 8x + 16$$

c. $(2x + 5)^2$

$$a = 2x \quad b = 5$$

$$(2x)^2 + 2(2x)(5) + 5^2$$

$$4x^2 + 20x + 25$$

Checkpoint: Find the product

1. $(x + 9)^2$

$$(x+9)(x+9)$$

$$x^2 + 18x + 81$$

2. $(7a - 6)^2$

$$a = 7a \quad b = 6$$

$$(7a)^2 - 2(7a)(6) + 6^2$$

$$49a^2 - 84a + 36$$

Sum and Difference Pattern

$$(a + b)(a - b) = a^2 - b^2$$

Example 2: Find the product.

a. $(x + 5)(x - 5)$

FOIL

$$x^2 + 5x - 5x - 25$$

$$x^2 - 25$$

b. $(2x + 3)(2x - 3)$

$$a = 2x \quad b = 3$$

$$(2x)^2 - (3)^2$$

$$4x^2 - 9$$

c. $(4 - w)(4 + w)$

$$a = 4 \quad b = w$$

$$(4)^2 - (w)^2$$

$$16 - w^2$$

Checkpoint: Find the product.

3. $(5m + 10)(5m - 10)$

$$a = 5m \quad b = 10$$

$$(5m)^2 - (10)^2$$

$$25m^2 - 100$$

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Multiplying Functions

Perform the indicated operations using the functions $f(x) = 3x + 2$ and $g(x) = 3x - 4$

a) $f(x) \cdot g(x)$

$$(3x+2)(3x-4)$$

$$\text{FOIL} \rightarrow 9x^2 + 6x - 12x - 8$$

$$\boxed{9x^2 - 6x - 8}$$

b) $f(x) + g(x)$

$$(3x+2) + (3x-4)$$

$$\boxed{6x - 2}$$

c) $(f(x))^2$

$$(3x+2)^2 = (3x+2)(3x+2)$$

$$9x^2 + 6x + 6x + 4$$

$$\boxed{9x^2 + 12x + 4}$$